

Se asume siempre que estamos trabajando en un espacio de probabilidad  $(\Omega, \mathcal{A}, P)$ . We also assume that the notation makes sense, so for instance, if we are talking about a martingale, there is a filtration, etc.. Due on Wednesday 3/10/2018.

- 1)** Use the Radon-Nikodym Theorem to prove the existence of the conditional expectation  $E(f|\mathcal{B})$ , for  $f \in L^1$ .
- 2)** Prove that if  $f \in L^1$ , then  $\{E(f|\mathcal{A}_n)\}_{n \geq 0}$  is U.I.. You may use standard measure theoretic results without proof. You may, or may not, use Chebyshev-Markov.