Seminario de Análisis y Aplicaciones

Viernes, 26 de febrero de 2021

11:30 h., ONLINE - URL: https://zoom.us/j/97431429382

Carmelo Puliatti

Euskal Herriko Unibersitatea

Blow-ups of caloric measure and applications to two-phase problems

Resumen:

Let Ω^+ and Ω^- be disjoint time-varying domains in $\mathbb{R}^n_x \times \mathbb{R}_t$, $n \geq 2$, and let ω^\pm denote their associated caloric measures. Under appropriate mild non-degeneracy and regularity hypotheses on Ω^\pm , mutual absolute continuity of ω^+ and ω^- on $E \subset \partial \Omega^+ \cap \partial \Omega^- \cap \operatorname{supp} \omega^+$ implies that the parabolic Hausdorff dimension of $\omega^+|_E$ is n+1 and the parabolic blow-ups of ω^+ at ω^+ -a.e. point of E are equal to a constant multiple of the parabolic (n+1)-Hausdorff measure restricted to hyperplanes containing a line parallel to the time-axis.

This is a parabolic analogue of a result of Kenig, Preiss and Toro, and its proof involves a set of techniques based on parabolic tangent measures. These methods, which I am going to discuss in my talk, also have other geometric applications, amongst which a caloric version of a theorem of Tsirelson about triple-points.

This is a joint work with Mihalis Mourgoglou.

ICMAT CSIC-UAM-UC3M-UCM Departamento de Matemáticas. U.A.M.



