

# SEMINARIO DE ANÁLISIS Y APLICACIONES

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11:30 h., ONLINE - URL: <https://zoom.us/j/97951668479>

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The two-phase problem for harmonic measure in VMO via jump formulas for the Riesz transform

## Resumen:

Let  $\Omega^+ \subset \mathbb{R}^{n+1}$  be an NTA domain and let  $\Omega^- = \mathbb{R}^{n+1} \setminus \overline{\Omega^+}$  be an NTA domain as well. Denote by  $\omega^+$  and  $\omega^-$  their respective harmonic measures. Assume that  $\Omega^+$  is a  $\delta$ -Reifenberg flat domain for some  $\delta > 0$  small enough.

In a joint work with X. Tolsa we show that  $\log \frac{d\omega^-}{d\omega^+} \in \text{VMO}(\omega^+)$  if and only if  $\Omega^+$  is vanishing Reifenberg flat,  $\Omega^+$  and  $\Omega^-$  have joint big pieces of chord-arc subdomains, and the inner unit normal of  $\Omega^+$  has vanishing oscillation with respect to the approximate normal.

This result can be considered as a two-phase counterpart of a more well known related one-phase problem for harmonic measure solved by Kenig and Toro.

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